



AMERICAN NATIONAL STANDARD

Methods for the Experimental Determination of Mechanical Mobility. Part 1: Basic Definitions and Transducers

Secretariat:

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Approved on 10 October 1979:

American National Standards Institute, Inc.

Abstract

This standard is the first part of a series of live standards covering the experimental determination of mechanical mobility of structures by a variety of methods appropriate for different test situations. The present Part I of this series covers basic concepts and definitions and serves as a guide for the selection, calibration, and evaluation of the transducers and instruments used in mobility measurements. The material in Part I is common to most mobility measurement tasks. This document supersedes ANSI Standard S2.6-1963 (R1976).

The future parts of this series will cover specific mobility measurement situations such as the use of steady-state rectilinear excitation, steady-state torsional excitation, measurements of the entire mobility matrix using steady-state excitation, and mobility measurements using impact excitation, as well as other forcing functions which use Fourier transform techniques for data reduction.

The present document (Part I of this series) has four appendices containing selected references to the literature, a discussion of the relationships between mechanical mobility and impedance, a discussion of mobility as a frequency response function, and conversion factors from S1 to conventional English units as applicable to mobility and related ratios.

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AMERICAN NATIONAL STANDARD

**Methods for the Experimental Determination of
Mechanical Mobility.**

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Part I: Basic Definitions and Transducers

ABSTRACT

This standard is the first part of a series of five standards covering the experimental determination of mechanical mobility of structures by a variety of methods appropriate for different test situations. The present Part I of this series covers basic concepts and definitions and serves as a guide for the selection, calibration, and evaluation of the transducers and instruments used in mobility measurements. The material in Part I is common to most mobility measurement tasks. This document supersedes ANSI Standard S2.6-1963(R1976).

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AMERICAN NATIONAL STANDARDS ON ACOUSTICS

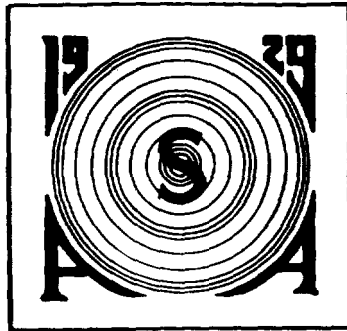
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FOREWORD

[This Foreword is not a part of American National Standard Methods for the Experimental Determination of Mechanical Mobility. Part I: Basic Definitions and Transducers, S2.31-1979.]

This standard has been developed under the jurisdiction of American National Standards Committee S2 using the American National Standards Institute (ANSI) Standards Committee Procedure. The Acoustical Society of America holds the Secretariat for Committee S2. This standard has been approved for publication by ANSI and by the Acoustical Society of America Committee on Standards (ASACOS).

The scope of Standards Committee S2 on Mechanical Shock and Vibration, under whose jurisdiction this standard was prepared, is as follows:

Standards, specifications, methods of measurement and test, and terminology in the fields of mechanical shock and vibration, but excluding those aspects which pertain to biological safety, tolerance, and comfort.

At the time this standard was submitted to Standards Committee S2 for approval, the membership was as follows:

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Working Group S2-74 on Measurement of Mechanical Mobility, which prepared this standard, has the following membership:

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Suggestions for improvement of this standard will be welcomed. They should be sent to the Standards Secretariat, Acoustical Society of America, 335 East 45th Street, New York, NY 10017.

CONTENTS

INTRODUCTION	1
1 PURPOSE AND SCOPE	2
1.1 Purpose.....	2
1.2 Scope.....	2
1.3 Related standards	2
2 DEFINITIONS	2
2.1 Mobility	2
2.2 Blocked impedance.....	3
2.3 Free impedance.....	3
2.4 Other forms of mobility.....	4
3 BASIC REQUIREMENTS FOR FORCE AND MOTION MEASUREMENT TRANSDUCERS	4
3.1 General	5
3.2 Requirements for motion measurement transducers	5
3.3 Requirements for force measurement transducers.....	6
3.4 Requirements for impedance heads and attachments to the structure under test.....	6
4 CALIBRATION OF THE MEASURING TRANSDUCERS.....	7
5 BASIC TRANSDUCER CALIBRATIONS	7
5.1 General	8
5.2 Sensitivity.....	8
5.3 Electrical impedance	8
6 SUPPLEMENTAL CALIBRATIONS.....	9
6.1 General	9
6.2 Dimensions	9
6.3 Mass	10
6.4 Effective end mass of force transducers and mechanical impedance transducers	10
6.5 Stiffness of force transducers and mechanical impedance transducers	10
6.6 Polarity.....	10
6.7 Frequency response.....	11
6.8 Amplitude linearity	11
6.9 Supplemental calibrations necessitated by environmental and secondary effects.....	11
APPENDICES	
APPENDIX A References	12

APPENDIX B Discussion of mobility and blocked impedance12

APPENDIX C Mobility as a frequency response function 13

APPENDIX D Nomenclature—SI and conventional English units.....13

TABLES

TABLE I Equivalent definitions to be used for various kinds of output/input ratios.....4

TABLE II Summary of calibrations and tests7

FIGURES

FIG. 1 Mobility plot.....3

FIG. 2 Accelerance magnitude plot corresponding to Fig. 15

FIG. 3 Dynamic compliance magnitude plot corresponding to Fig. 16

American National Standard

Methods for the Experimental Determination of Mechanical Mobility.

Part I: Basic Definitions and Transducers

INTRODUCTION

The dynamic characteristics of structures can be determined from measurements of mobility or of the related frequency response functions called accelerance and dynamic compliance. These frequency response functions describe the relationship of the motion response (output) of a structure to a force input as a function of frequency. This response ratio has a magnitude equal to the ratio of the output to the input amplitudes and a phase equal to the phase of the output relative to the input. Traditionally, the input force in mobility measurements has been sinusoidal, but recent advances in technology have made it possible to use random or transient forcing functions as described in detail in Appendix C.

Mobility measurements are usually made with force transducers and accelerometers within the frequency range of 5–5000 Hz, although special applications may require other frequency ranges and/or other types of transducers.

Mobility measurements are used for:

- (1) Predicting the dynamic response of structures to arbitrary input forces,
- (2) Determining structural resonance modes (natural frequencies, mode shapes, and damping ratios),
- (3) Determining the dynamic interaction of interconnected structures and equipment, and
- (4) Determining dynamic properties of materials or composites (complex modulus of elasticity).

The *complete* determination of the dynamic characteristics of some structures may require the measurement of rectilinear forces and motions as well as the measurement of moments and rotational motions about three mutually perpendicular axes. The measurement of the 21 independent^{a)} terms, each a function of frequency, yields a 6×6 mobility matrix at each point of interest. This is further complicated by the fact that each of the N points of interest in a structure has a 6×6 mobility matrix. Thus, the system has an overall matrix of size $6N \times 6N$. There are $36N^2$ elements in all of which $(18N^2 + 3N)$ need to be mea-

sured. Much less detail is usually required for practical applications. Often, it is sufficient to measure the driving point mobility and the transfer mobilities determined from the application of a single force in one direction and the measurement of rectilinear motions in the same or other directions at the same point or other points on the structure. For example, one or two such forcing positions may provide sufficient information to determine specific modal parameters of the structure. An alternative to the use of a single driving point and multiple response points is sometimes more practical when an impact method is used to apply the input force. This alternative involves the application of forces, one at a time, at all the points and directions of interest and measuring the rectilinear response motion at a single point and single direction for each of the force applications.

In order to simplify the use of this standard in performing the varied mobility measurement tasks encountered in practice, this standard will be issued in five separate parts:

Part I (the present document) covers basic definitions and transducers. This material is common to most mobility measurement tasks.

Part II will cover mobility measurements using steady-state translational excitation at a single point.

Part III will cover mobility measurements using steady-state rotational excitation at a single point. This is primarily intended for rotor torsional resonance predictions.

Part IV will cover mobility measurements of the entire mobility matrix using steady-state excitation.

Part V will cover mobility measurements using impact excitation as well as other forcing functions which use Fourier transform techniques for data reduction.

Mechanical mobility is defined as the ratio of the phasor of the velocity to the phasor of the applied force.^{b)} More detailed definitions of mechanical mobility and other measures of the dynamic characteristics of structures are given in Sec. 2 of this standard. The motion measurements are usually made with accelero-

^{a)}Mobility matrices are usually symmetric, at least for linear, bilateral networks.

^{b)}Henceforth, the shorter terms "velocity phasor" and "force phasor" will be used for the phasors of the velocity and force. The definition of these phasors is given in Appendix C.